Contribution from the Department of Applied Chemistry, Faculty of Engineering, Kumamoto University, Kurokami, Kumamoto 860, Japan

Ab Initio MO Study of Palladium-Assisted Nucleophilic Attack on a Coordinated Olefin: Semiquantitative Understanding of the Reaction and the Mechanism of Palladium Acceleration

Shigeyoshi Sakaki,* Katsuhiko Maruta, and Katsutoshi Ohkubo

Received January 6, 1987

Aminopalladation of olefins is theoretically investigated here as an example of palladium-assisted nucleophilic attack on a coordinated olefin by an ab initio MO method and energy decomposition analysis. In $[PdF_3(C_2H_4)]^-$ and $PdF_2(NH_3)(C_2H_4)$, the trans attack of a nucleophile, NH₃, on the coordinated ethylene causes significant destabilization. In $[PdF(NH_3)_2(C_2H_4)]^+$ and $[PdF(PH_3)_2(C_2H_4)]^+$, on the other hand, the trans attack of NH₃ proceeds easily with a rather small activation barrier. These results suggest that the active species is a cationic palladium(II)-olefin complex. Analyses of the interaction energy and electron distribution indicate that not only charge transfer from the nucleophile, NH₃, to C_2H_4 but also polarization of the Pd-C₂H₄ moiety is important to the reaction. Orbital mixings for frontier orbitals proposed here clearly elucidate why the cationic complex structure change during the reaction.

Introduction

While unactivated olefins do not undergo nucleophilic attack, their coordination to appropriate transition-metal ions can often accelerate the reaction.¹ Such metal-assisted nucleophilic attack is involved as a key step in many catalytic reactions and organic syntheses with transition metals.^{1,2} In this type of nucleophilic attack, information about the origin of the acceleration by metal coordination, factors contributing to the activation of olefins, and changes in electron distribution and geometry during nucleophilic attack are important and useful in improving the reactivity of transition-metal complexes and in finding good catalysts for the nucleophilic attack. Some of these aspects can be effectively investigated with an MO method, and therefore, during the last decade several MO studies have been carried out on metal-assisted nucleophilic attack.³ In particular, Eisenstein and Hoffmann proposed an elegant explanation of metal acceleration by their EH-MO approach.^{3b} Up to the present time, however, very little has been determined on a quantitative level about metal-assisted nucleophilic attack, such as the energetics, activation barrier, and changes in geometry, electron distribution, and bonding.

In this work, ab initio MO calculations are carried out on palladium(II)-assisted nucleophilic attack on a coordinated ethylene. The palladium(II) complex is one of the most useful metal complexes in various catalytic reactions and organic syntheses, 1,2 such as the Wacker process, aminopalladation of olefins,⁴ palladium-assisted alkylation of olefins,⁵ and so on, 4c,6

- The following review articles have been published concerning this issue:
 (a) Davies, S. G.; Green, M. L. H.; Mingos, D. M. P. Tetrahedron 1978, 34, 3047.
 (b) Houghton, R. P. Metal Complexes in Organic Chemistry; Cambridge University Press: Cambridge, England, 1979; Chapter 4.
- (2) (a) Hartley, F. R. The Chemistry of Platinum and Palladium; Applied Science: London, 1973. (b) Trost, B. M. Tetrahedron 1977, 33, 2615.
 (c) Kochi, J. K. Organometallic Mechanisms and Catalysis; Academic: New York, 1978; Chapter 5. (d) Heck, R. F. Acc. Chem. Res. 1979, 12, 146. (e) Bäckvall, J.-E. Ibid. 1983, 16, 335.
- (a) Sakaki, S.; Nishikawa, M.; Ohyoshi, A. J. Am. Chem. Soc. 1980, 102, 4062.
 (b) Einsenstein, O.; Hoffmann, R. Ibid. 1980, 102, 6148; 1981, 103, 4308.
 (c) Bäckvall, J.-E.; Björkman, E. E.; Petterson, L.; Siegbahn, P. Ibid. 1984, 106, 4369; 1985, 107, 7265.
 (d) Fujimoto, H.; Yamasaki, T. Ibid. 1986, 108, 578.
 (e) Sakaki, S.; Maruta, K.; Ohkubo, K. J. Chem. Soc., Dalton Trans. 1987, 361.
- (4) (a) Åkermark, B.; Bäckvall, J.-E.; Siirala-Hansén, K.; Sjöberg, K.; Zetterberg, K. Tetrahedron Lett. 1974, 1363. (b) Åkermark, B.; Bäckvall, J.-E. Ibid. 1975, 819. (c) Hegedus, L. S.; Siirala-Hansén, K. J. Am. Chem. Soc. 1975, 97, 1184. (d) Bäckvall, B. Tetrahedron Lett. 1978, 163. (e) Bäckvall, J.-E.; Björkman, E. E. J. Org. Chem. 1980, 45, 2893. (f) Bäckvall, J.-E.; Björkman, E. E.; Byström, S. E. Tetrahedron Lett. 1982, 943. (g) Bäckvall, J.-E.; Byrström, S. E. J. Org. Chem. 1982, 47, 1126.
- (5) (a) Hayashi, T.; Hegedus, L. S. J. Am. Chem. Soc. 1977, 99, 7093. (b) Murahashi, S.; Yamamura, M.; Mita, N. J. Org. Chem. 1977, 42, 2870.
 (c) Hegedus, L. S.; Hayashi, T.; Darlington, W. H. J. Am. Chem. Soc. 1978, 100, 7747. (d) Kurosawa, H.; Asada, N. Tetrahedron Lett. 1979, 255. (e) Hegedus, L. S.; Williams, R. E.; McGuire, M. A.; Hayashi, T. J. Am. Chem. Soc. 1980, 102, 4973.





in which nucleophilic attack on an olefin is involved as a key step. This is the reason the palladium(II) system is examined here. Of the many palladium(II)-assisted reactions, aminopalladation of olefins would appear to be the easiest for a theoretical study, because the nucleophile is a neutral amine and the reaction course (trans attack of the nucleophile) has been verified experimentally.^{4d,e} However, several issues are still ambiguous in this reaction: first, the identity of the active species, and second, the reason for the extreme facility of this reaction. For instance, the reaction can proceed even at -40 to -50 $^{\circ}\mathrm{C}.^{4b,d}$ In this theoretical work, we hope to answer the above-mentioned questions, i.e., (a) to elucidate the mechanism of palladium acceleration and the factors contributing to the activation of olefins, (b) to clarify the nature of the active species, and (c) to estimate the activation barrier of the reaction. The emphasis, and point of departure from previous work, is on presenting a semiquantitative understanding of palladium-assisted nucleophilic attack, including changes in

^{(6) (}a) Henry, P. M. Acc. Chem. Res. 1973, 6, 16; J. Am. Chem. Soc. 1972, 94, 7305; J. Org. Chem. 1967, 32, 2575; 1973, 38, 1681; 1974, 39, 3871.
(b) Still, J. K.; James, D. E.; Hines, L. F. J. Am. Chem. Soc. 1973, 95, 5062. (c) Bäckvall, J.-E. J. Chem. Soc., Chem. Commun. 1977, 413. (d) Bäckvall, J. E.; Åkermark, B.; Ljunggren, S. O. J. Am. Chem. Soc. 1979, 101, 2411. (e) Kurosawa, H.; Majima, T.; Asada, N. Ibid. 1980, 102, 6996.



Figure 1. Optimized structure of $PdF_2(NH_3)(C_2H_4)$ (bond lengths in angstroms and bond angles in degrees). Values in parentheses are assumed values taken from the optimized structure of the fragment molecule, ^{13a} the value in brackets is the experimental value of $[PdCl_2(C_2 [H_4)]_{2}$,¹⁴ and the values marked "Hay" are the optimized values for $[PdCl_3(C_2H_4)]^-$ by Hay.¹⁵

total energy, geometry, and electron distribution.

Computational Details

All-electron ab initio MO calculations were carried out on [PdF₃- $(C_2H_4)^-$ (1), PdF₂(NH₃)(C₂H₄) (2), [PdF(NH₃)₂(C₂H₄)]⁺ (3), and [PdF(PH₃)₂(C₂H₄)]⁺ (4) (Chart I), and the reaction systems of the nucleophilic attack of NH₃ on the coordinated ethylene in 1-4 (Chart II), by using the IMSPAK⁷ and Gaussian 82⁸ program systems. Two kinds of basis sets were employed. In the smaller basis (SB) set, MIDI-19a and STO-3G¹⁰ were used for palladium and ligand atoms, respectively, where three p-type primitives,¹¹ contracted to minimal, were added to MIDI-1 to describe the 5p orbital of palladium. With this basis set, geometry optimization was carried out. In the larger basis (LB) set, the MIDI-1 set for palladium was augumented with one diffuse Gaussian d orbital (exponent 0.11)¹² and then contracted to [333321/33321/3211]. For ligand atoms, the usual MIDI-1 sets were used.^{9b,c} This LB set was employed in a discussion of energetics, bonding, and electron distribution.

Geometry optimization with parabolic fitting of total energies was carried out on some important bond distances and bond angles. For instance, the Pd—C, C=C, Pd—F, and Pd—N bond distances and the CH₂ bending angles were optimized in PdF₂(NH₃)(C₂H₄), with the remaining geometrical parameters of C₂H₄ and the structure of NH₃ being taken from the literature (optimized values with STO-3G set).¹³ Those optimized values agree well with experimental¹⁴ and optimized values¹⁵ of similar complexes, as compared in Figure 1. In the nucleophilic attack of NH₃ on PdF₂(NH₃)(C₂H₄), the C^{α}--NH₃ distance was taken as a reaction coordinate and geometrical parameters such as the C^{α} - C^{β} and Pd-C^{β} distances, the NC^{α}C^{β}, C^{α}C^{β}Pd, and zPdC^{β} angles (z = z axis), and the $C^{\alpha}H_2$ and $C^{\theta}H_2$ bendings were optimized independently (see Chart II for C^{α} , C^{β} , etc.).¹⁶ These values were adopted in the other palladi-

- (7) Morokuma, K.; Kato, S.; Kitaura, K.; Ohmine, I.; Sakai, S.; Obara, S. IMS Computer Center Program Library; Institute for Molecular Science: Okazaki, Japan, 1980; No. 0372.
- Binkley, J. S.; Frisch, M. J.; DeFrees, D. J.; Raghavachari, K.; (8)Whiteside, R. A.; Schlegel, H. B.; Pople, J. A. Gaussian 82; Carnegie-Mellon Chemistry Publishing Unit: Pittsburgh, PA, 1984
- (a) Sakai, Y.; Tatewaki, H.; Huzinaga, S. J. Comput. Chem. 1982, 3, (b) Tatewaki, H.; Huzinaga, S. Ibid. 1980, 1, 205. (c) For the hydrogen atom, the split-valence basis set proposed by Huzinaga-Dun-ning was used: Dunning, T. H.; Hay, P. J. In Method of Electronic
- (10) (a) Hehre, W. J.; Stewart, R. F.; Pople, J. A. J. Chem. Phys. 1969, 51, 2657.
 (b) Hehre, W. J.; Stewart, R. F.; Pople, J. A. J. Chem. Phys. 1969, 51, 2657.
 (b) Hehre, W. J.; Ditchfield, R.; Stewart, R. F.; Pople, J. A. Ibid. 1970, 52, 2769.
- The coefficients and exponents are taken to be the same as those of the (11)Pd 5s orbital of the MINI-1 set.
- (12) This value was obtained by the even-tempered criterion.
- (13) (a) Binkley, J. S.; Pople, J. A.; Hehre, W. J. J. Am. Chem. Soc. 1980, 102, 939. Gordon, M. S.; Binkley, J. S.; Pople, J. A.; Pietro, W. J.; Hehre, W. J. *Ibid.* 1982, 104, 2797. (b) In $[PdF(PH_3)_2(C_2H_4)]^+$, the Pd—PH₃ distance was taken from the experimental structure of a similar complex: Ferguson, G.; McCrindle, R.; McAlees, A. J.; Parvez, M. Acta Crystallogr., Sect. B: Struct. Crystallogr. Cryst. Chem. 1982, B38. 3679.
- (14) Dempsey, J. N.; Baenziger, N. C. J. Am. Chem. Soc. 1955, 77, 4984
- (15) Hay, P. J. J. Am. Chem. Soc. 1981, 103, 1390.

Table I. Energy Decomposition Analysis (kcal/mol) of the Interaction between C_2H_4 and PdF_nL_{3-n} $(n = 1-3, L = NH_3 \text{ or } PH_3)$ and Changes in Mulliken Population Caused by the Coordination of Ethylene

	[PdF ₃ -	PdF ₂ -	$[PdF(NH_3)_2-$	[PdF(PH ₃) ₂ -					
	$(C_2H_4)]^-$	$(\mathrm{NH}_3)(\mathrm{C}_2\mathrm{H}_4)$	$(C_2H_4)]^+$	$(C_2H_4)]^+$					
Energy Decomposition Analysis									
BE	-16.1	-18.0	-24.2	-23.5					
DEF ^a	1.4	1.4	1.4	1.4					
INT	-17.5	-19.4	-25.6	-24.9					
ES	-45.5	-46.2	-46.2	-47.9					
EX	55.7	55.0	54.8	59.3					
FCTPLX	-10.8	-15.4	-20.6	-22.6					
BCTPLX	-11.9	-9.4	-11.7	-11.7					
R	-5.0	-3.4	-1.9	-2.0					
Changes in Mulliken Population ^b									
Pd	+0.12	+0.23	+0.28	+0.26					
C ₂ H₄	-0.11	-0.24	-0.34	-0.38					
cis ligand	-0.01 (F)	0 (F)	+0.02 (F)	+0.02 (F)					
-			+0.02 (NH ₃)	+0.03 (PH ₃)					
trans ligand	0 (F)	+0.01 (NH ₃)	+0.02 (NH ₃)	+0.07 (PH ₃)					

^a The same geometry of C_2H_4 is assumed in these complexes (see text). The structure of the PdF_nL_{3-n} fragment was taken to be the same as the structure of the corresponding part in the total complex, and the DEF value of the PdF_nL_{3-n} fragment was not considered. ^b"+' means an increase in Mulliken population upon the coordination of ethylene, and "-" means a decrease in Mulliken population.

um(II)-ethylene complexes and reaction systems for NH3 attack, to save CPU time, because of the large systems examined.

In an attempt to investigate in detail the coordinate bond of ethylene to palladium and the interaction between the nucleophile, NH₃, and the palladium(II)-ethylene complex, the energy decomposition analysis proposed by Morokuma et al.¹⁷ was applied here. In this analysis, a total system is considered to consist of two parts; for instance, the palladiumethylene complex is composed of the ethylene ligand and the remaining palladium part, and the reaction system of the NH₃ nucleophilic attack is composed of the nucleophile, NH₃, and the palladium-ethylene complex. The binding energy (BE) is defined as stabilization of a total system, A-B, compared to separated fragments A and B taking their equilibrium structures, and it can be represented as

$$BE = E_t(A-B) - E_t(A)_{eq} - E_t(B)_{eq} = DEF + INT$$
$$DEF = \{E_t(A)_{dist} - E_t(A)_{eq}\} + \{E_t(B)_{dist} - E_t(B)_{eq}\}$$
$$INT = E_t(AB) - E_t(A)_{dist} - E_t(B)_{dist}$$

where the subscripts "eq" and "dist" mean the equilibrium and distorted structures, respectively. DEF (deformation energy) is the destabilization energy to deform A and B from their equilibrium structures to their distorted structures taken in the total system. INT (interaction energy) is the stabilization of the total system compared to the distorted fragments of A and B and is further divided into various chemically meaningful terms:

$$NT = ES + EX + FCTPLX + BCTPLX + R$$

ES and EX are the Coulombic electrostatic interaction and the exchange repulsion interaction, respectively. FCTPLX contains the charge transfer from the Lewis base, B, to the Lewis acid, A, the polarization of A, and their coupling term. BCTPLX contains the charge transfer from A to B, the polarization of B, and their coupling term, and R is the higher order remaining term. In the case of the palladium-ethylene complex, FCTPLX is defined so as to include the charge transfer from ethylene to the remaining palladium part, according to the general concept of the coordinate bond. In the reaction systems of NH₃ attack, FCTPLX is defined to include the charge transfer from the nucleophile, NH₃, to the palladium-olefin complex, considering the Lewis basicity of the nucleophile, NH₃.

Results and Discussion

The Coordinate Bond in Palladium-Ethylene Complexes. Before we start to discuss the nucleophilic attack of NH₃ on the coor-

- (16) During the reaction, the Pd-F, Pd-NH₃, and Pd-PH₃ distances were both point reaction, the full range flat the Hg-ligand distance was changed little by nucleophilic attack on ethylene coordinated to Hg.^{3e} (a) Morokuma, K. *Int. J. Quantum Chem.* **1976**, *10*, 325. (c) Kitaura, K.; Norokuma, K. *Int. J. Quantum Chem.* **1976**, *10*, 325. (c) Kitaura, K.;
- (17)Sakaki, S.; Morokuma, K. Inorg. Chem. 1981, 10, 2292.



Figure 2. Energy change caused by the NH₃ nucleophilic attack on $PdF_nL_{3-n}(C_2H_4)$ (L = NH₃ or PH₃; n = 1-3; $\Delta E_t = E_t(PdF_nL_{3-n}-(C_2H_4)-NH_3) - E_t(PdF_nL_{3-n}(C_2H_4)) - E_t(NH_3))$.

dinated ethylene, the coordinate bond in the palladium-ethylene complexes will be investigated, in order to obtain some useful information on the relation between the coordinate bond and the reactivity. Results of energy decomposition analysis are listed in Table I, together with changes in Mulliken population caused by the coordination of ethylene. The binding of ethylene becomes stronger in the order $[PdF_3(C_2H_4)]^- < PdF_2(NH_3)(C_2H_4) <$ $[PdF(PH_3)_2(C_2H_4)]^+ < [PdF(NH_3)_2(C_2H_4)]^+$. It is noted that although the ES, EX, and BCTPLX interactions do not exhibit large changes among the complexes examined, the FCTPLX stabilization increases with increasing binding energy except for $[PdF(PH_3)_2(C_2H_4)]^+$. This complex suffers more from the EX repulsion than $[PdF(NH_3)_2(C_2H_4)]^+$, probably due to larger steric repulsion between ethylene and bulky PH₃ ligands, which leads to the binding energy of this complex being slightly smaller than that of $[PdF(NH_3)_2(C_2H_4)]^+$ despite the greater FCTPLX stabilization in the former.

Corresponding to the increasing order of the FCTPLX stabilization, the electron population of C_2H_4 decreases in the order I > II > III > IV, as shown in Table I. Electron populations of other ligands exhibit interesting changes upon ethylene coordination; although the electron populations of F and NH₃ are affected little by ethylene coordination, the electron population of the trans PH3 ligand is increased somewhat, indicating that ethylene coordination hardly influences electron donation from F⁻ and NH₃ to Pd but weakens electron donation from trans PH₃ to Pd. This difference between F⁻, NH₃, and PH₃ is suggestive of the nature of ligands. Hard ligands such as F and NH, have a tendency to keep the strength of electron donation constant, but a soft ligand like PH₃ has an ability to control the extent of electron donation from PH₃ to Pd so as to keep the electron density of the central metal at the appropriate value. These features of coordinate bond and ligand character will be discussed later in relation to the palladium acceleration of nucleophilic attack.

Changes in Total Energy and Geometry during NH₃ Attack. Changes in the total energy, ΔE_t , of the reaction system $[PdF_nL_{3-n}(C_2H_4)] \leftarrow NH_3$ (n = 1-3; $L = NH_3$ or PH₃) are given as a function of the C^{α} —N distance in Figure 2, where a standard (zero energy) is taken for $R_{C^{\alpha}-N} = \infty$. Approach of the nucleophile, NH₃, to free C_2H_4 , $[PdF_3(C_2H_4)]^-$, and $PdF_2(N-H_3)(C_2H_4)$ yields substantial destabilization. On the other hand, attack of NH₃ on $[PdF(NH_3)_2(C_2H_4)]^+$ and $[PdF(PH_3)_2(C_2H_4)]^+$ proceeds very easily with activation barriers of ca. 8 and 6 kcal/mol, ^{18a,b} respectively. These values, of course, must be



Figure 3. Geometry change of the palladium-ethylene moiety along the reaction coordinate for nucleophilic addition of NH_3 to the coordinated ethylene (bond lengths in angstroms and bond angles in degrees). Ligand parts are omitted, because those positions are fixed during the reaction.

corrected by introducing electron correlation effects and basis set superposition error (BSSE), which will be briefly discussed later. Even though these activation energies should be corrected, the above results suggest that a cationic palladium(II)-olefin complex is an active species of this reaction.^{18c,d} In fact, the palladiumassisted alkylation and amination of olefins are accelerated very much by addition of excess amine, which should form a cationic palladium complex.^{4c,d,f,5a,c-e} Furthermore, Kurosawa and his collaborators have reported that the facile attack of nucleophiles on the coordinated olefins occurs in isolated cationic palladium(II) complexes.^{5d,6e} These experimental results are consistent with our suggestion that the active species is a cationic palladium(II)-olefin complex.

The geometry change of the palladium-ethylene complex along the reaction coordinate $(R_{C^{\alpha}-N})$ is displayed in Figure 3. Several interesting features are found; when NH₃ approaches C_2H_4 , the $C^{\alpha}-C^{\beta}$ and Pd- C^{α} bond distances are lengthened, the Pd- C^{β} distance is shortened, and simultaneously the $C^{\alpha}H_2$ and $C^{\beta}H_2$ bendings are increased. These changes in geometry correspond with the conversions of the $C^{\alpha}=C^{\beta}$ double bond to the $C^{\alpha}-C^{\beta}$ single bond and of the η^2 -coordinated ethylene to the η^1 -coordinated alkyl group. Another interesting feature is that these geometrical changes arise simultaneously and smoothly, suggesting that the bond formation and bond breaking occur in a concerted manner.

Near the transition state (at $R_{C^{\alpha}-N} = 2.0$ Å), the $C^{\alpha}-C^{\beta}$ distance lenghtens by only 0.04 Å, about 20% of the total increase, if the $C^{\alpha}-C^{\beta}$ distance of the product is taken as 1.54 Å (the standard value for the C-C single bond).¹⁹ The $C^{\alpha}H_2$ and $C^{\beta}H_2$ bendings increase by about 20° at $R_{C^{\alpha}-N} = 2.0$ Å, which corresponds to about 40% of the total increase in the CH₂ bending, if the product is assumed to have tetrahedral bond angles around the C^{α} and C^{β} atoms. These geometrical changes indicate a signal that the transition state is not late but rather early, which will be also supported by the other results, as discussed later.

Changes in Electron Distribution during the Reaction. Changes in the Mulliken population caused by NH_3 attack are given in Figure 4, as a function of the reaction coordinate. Approach of NH_3 to ethylene significantly decreases the electron population of NH_3 and substantially increases the electron population of the

^{(18) (}a) These values correspond to the destabilization in total energy relative to that of R_{C^α-N} = 3.0 Å. Although this estimation of the activation barrier is not correct, strictly speaking, the value estimated does not seem unreasonable, because both structures at R_{C^α-N} = 3.0 and 2.5 Å exhibit almost the same E₁ value in [PdF(NH₃)₂(C₂H₄)]⁺. (b) The products obtained from [PdF(NH₃)₂(C₂H₄)]⁺ and [PdF(PH₃)₂(C₂H₄)]⁺ are less stable than the reactants at R_{C^α-N} = 3.0 Å. This rather unreasonable feature might arise from the neglect of the electron correlation effect and solvation effect, no optimization of the N—H bond length, etc. (c) Introducing an electron correlation energy with the MP2 method stabilizes the product relative to the reactant; for the model system [PdF(C₂H₄)]⁻→NH₃, ΔE_{corr} = E_{corr}(R_{C^α-N} = 1.6 Å) - E_{corr}(R_{C^α-N} = 3.0 Å) = -7.0 kcal/mol. Even if this value is taken into consideration for [PdF₃(C₂H₄)]⁻→NH₃ and PdF₂(NH₃)(C₂H₄)→NH₃, effective stabilization cannot be expected at their product sides. (d) When the reactivities of cationic, neutral, and anionic palladium(II)-olefin complexes with a polar reagent are compared, differences in BSSE, solvation effect, electron correlation, and so on must be taken into consideration. Some of them are being investigated now.

⁽¹⁹⁾ Sutton, L. E., Ed. Spec. Publ.-Chem. Soc. 1965, No. 18.



Figure 4. Changes in Mulliken population (change = $\rho(Pd-ethylene - NH_3) - \rho(Pd-ethylene) - \rho(NH_3)$) along the reaction coordinate for nucleophilic addition of NH₃ to the coordinated ethylene.



Figure 5. Difference density maps of the reaction system $[PdF(PH_3)_2 (C_2H_4)]^+ - NH_3$ (difference = $\rho([PdF(PH_3)_2(C_2H_4)]^+ - NH_3) - \rho - ([PdF(PH_3)_2(C_2H_4)]^+) - \rho(NH_3))$: (---) increase in the density of 0.001, 0.005, 0.01, and 0.05; (---) decrease in the density of -0.001, -0.005, -0.01, and -0.05; (---) 0.0.

 C_2H_4 moiety, suggesting the importance of the charge transfer from NH_3 to C_2H_4 . In spite of this significant charge transfer from NH_3 to C_2H_4 , the transferred electrons from NH_3 do not distribute uniformly over the C2H4 moiety but accumulate on the C^{β} atom, as shown by the considerable increase of the C^{β} atomic population and the remarkable decrease of the C^{α} atomic population (see Figure 4). These changes imply that not only the simple charge transfer from NH₃ to C₂H₄ but also polarization of the C_2H_4 moiety takes place in the reaction. Approach of NH₃ to C_2H_4 also gradually increases the electron population of the PdF_nL_{3-n} group (Figure 4), which means that the charge transfer from C_2H_4 to PdF_nL_{3-n} simultaneously occurs. However, the atomic population of palladium hardly increases, especially in the case of $[PdF(PH_3)_2(C_2H_4)]^+$. Again, this result cannot be explained by the simple charge transfer from C_2H_4 to PdF_nL_{3-n} but by the polarization of PdF_nL_{3-n} coupled with the charge transfer from C_2H_4 to PdF_nL_{3-1}

The above-described changes in electron distribution are represented more clearly by the difference density map of Figure 5A, in which the difference density of the $[PdF(PH_3)_2(C_2H_4)]^+ - NH_3$ system is given as a typical example. Electron density decreases in the region of the lone-pair orbital of NH₃, which is in accordance

Chart III



with the charge transfer from NH_3 to C_2H_4 . In the C_2H_4 moiety, electron density decreases near the C^{α} atom but increases near the C^{β} atom, indicating the polarization of this moiety. Near the Pd atom, however, complicated changes of electron distribution are found; the electron density decreases in the region pointing to the C^{β} atom, probably because the electron density of the d_{σ} orbital might be reduced so as to weaken the EX repulsion with the accumulated electron density on the C^{β} atom. In the other region around the Pd atom, the electron density is increased, due to the charge transfer from C^{β} to Pd. Also, a very small but nonnegligible increase of the electron density is found at the region of the lone pair of the trans ligand. These features found in the difference density map suggest that the nucleophilic attack causes both simple charge transfer from C_2H_4 to Pd and polarization of PdF_nL_{3-n} . In summary, four kinds of redistribution of electrons arise from the nucleophilic attack, as schematically depicted in Chart III; the first is the charge transfer from NH_3 to C_2H_4 , the second is the polarization of C_2H_4 , the third is the charge transfer from C_2H_4 to PdF_nL_{3-n} , and the last is the polarization of PdF_nL_{3-n} .

Changes in electron distribution will now be compared among the reaction systems examined. As shown in Figure 6, the electron population of the nucleophile, NH₃, decreases with increasing reactivity of the complex, i.e., $[PdF_3(C_2H_4)]^- > PdF_2(NH_3)(C_2H_4)$ > $[PdF(NH_3)_2(C_2H_4)]^+ > [PdF(PH_3)_2(C_2H_4)]^+$, indicating the importance of charge transfer from NH_3 to C_2H_4 . The electron population of the PdF_nL_{3-n} group also increases linearly with increasing reactivity, whereas electron populations of both C2H4 and Pd increase in the order $[PdF_3(C_2H_4)]^- < PdF_2(NH_3)(C_2H_4)$ < $[PdF(NH_3)(C_2H_4)]^+$ but then decrease for $[PdF(PH_3)_2^ (C_2H_4)$]⁺. From these results, it is considered important to the acceleration of nucleophilic attack that the PdF_nL_{3-n} group has enough ability to accept charge transfer from C_2H_4 . The reason for the importance of this charge transfer is unambiguous; the greater ability of the PdF_nL_{3-n} group to accept electrons results in smaller electron population of the C₂H₄ moiety, which strengthens charge transfer from the nucleophile, NH_3 , to C_2H_4 .



Figure 6. Changes in Mulliken population near the transition state $(R_{C^{\alpha}-N} = 2.0 \text{ Å}; \text{ change } = \rho(\text{Pd-ethylene}-\text{NH}_3) - \rho(\text{Pd-ethylene}) - \rho(\text{NH}_3)).$

Table II. Energy Decomposition Analysis (kcal/mol) of the Interaction between the Nucleophile NH_3 and the Palladium-Ethylene Complex

	•	1						
	free C₂H₄	[PdF ₃ - (C ₂ H ₄)] ⁻	$[PdF(NH_3)_2 - (C_2H_4)]^+$	$[PdF(PH_3)_2 - (C_2H_4)]^+$				
$\mathbf{D} = 20^{10}$								
$\kappa_{C^{\alpha}-N} = 3.0 \text{ A}$								
INT	0.6	3.2 (+2.6) ^a	$-8.1 (-8.7)^{a}$	-8.5 (-9.1) ^a				
ES	0.5	3.0 (+2.5)	-6.7 (-7.2)	-6.9 (-7.4)				
EX	2.5	2.6 (+0.1)	2.2 (-0.3)	2.2 (-0.3)				
FCTPLX	-2.2	-2.1 (+0.1)	-3.2(-1.0)	-3.2 (-1.0)				
BCTPLX	-0.2	-0.3 (-0.1)	-0.3 (-0.1)	-0.3 (0)				
R	0	0	-0.1 (-0.1)	-0.3 (-0.3)				
$R_{C^{\alpha}-N} = 2.0 \text{ A}$								
INT	28.2	21.9(-6.3)	-6.5 (-34.7)	-8.5 (-36.7)				
ES	-36.0	-34.4 (+1.6)	-45.8 (-9.8)	-46.2 (-10.2)				
EX	87.1	81.3 (-5.8)	71.6 (-15.5)	71.1 (-16.0)				
FCTPLX	-18.8	-20.7 (-1.9)	-26.6 (-7.8)	-27.6 (-8.8)				
BCTPLX	-6.3	-6.0 (+0.3)	-5.1 (+1.2)	-5.6 (+1.3)				
R	2.2	1.7 (-0.5)	-0.6 (-2.8)	-0.8 (-3.0)				

 $\,^{a}$ The difference from the interaction of free $C_{2}H_{4}$ with NH_{3} is given in parentheses.

In $[PdF(PH_3)_2(C_2H_4)]^+$, the atomic population of palladium only slightly increases in spite of the large increase in the electron population of the PdF(PH_3)_2 group, while the atomic population of palladium increases more in the other complexes than in the PH₃ analogue. This difference between the PH₃ complex and the others can be easily interpreted in terms of softness of PH₃; the PH₃ ligand has an ability to keep the Pd atomic population constant by controlling electron donation from PH₃ (vide supra), which would lead to the charge transfer from C₂H₄ to Pd in the PH₃ complex being greater than in the other complexes. The above discussion suggests that a neutral and soft ligand is desirable for the acceleration of nucleophilic attack.

Energy Decomposition Analysis between the Nucleophile (NH₃) and the Palladium-Ethylene Complex. For some typical reaction systems, the interaction between the nucleophile and palladiumethylene complexes was investigated with an energy decomposition analysis (EDA). As listed in Table II, the ES interaction is essential for the greater stabilization of the cationic palladiumethylene systems at $R_{C^{\alpha}-N} = 3.0$ Å, which seems reasonable because the electrostatic interaction is generally important to long-range interaction. At $R_{C^{\alpha}-N} = 2.0$ Å, the ES, EX, and FCTPLX interactions become considerably stronger, while the increases in the BCTPLX and R stabilizations are very small.

Table III. Changes in Mulliken Population Caused by the NH_3 Attack on $[PdF(PH_3)_2(C_2H_4)]^{+\alpha}$

	total	EX	FCTPLX	BCTPLX	R
$PdF(PH_3)_2^+$	+0.142	+0.012	+0.123	+0.004	+0.003
Pd	+0.003	+0.008	-0.002	+0.003	-0.006
F	+0.016	+0.001	+0.014	0	+0.001
cis PH ₃	+0.055	+0.001	+0.050	0	+0.004
trans PH3	+0.068	+0.002	+0.061	+0.001	+0.004
C_2H_4	+0.057	-0.012	+0.025	+0.015	+0.029
Cα	-0.134	-0.057	-0.133	-0.001	+0.057
C^{β}	+0.077	+0.035	+0.050	+0.013	-0.021
NH_3	-0.199	0.0	-0.147	-0.018	-0.034

^a The analysis is according to the EDA scheme ($R_{C^{\alpha}-N} = 2.0$ Å). "+" means an increase in Mulliken population upon the nucleophilic attack of NH₃, and "-" means a decrease.

Furthermore, the ES, EX, and FCTPLX interactions exhibit critical differences among the cationic palladium-ethylene complexes, the anionic complex, and free C_2H_4 ; the cationic palladium-ethylene complexes can receive significantly larger stabilization from the ES and FCTPLX terms than the free C_2H_4 and the anionic complex. On the other hand, the cationic complexes suffer less from the EX repulsion than the free C_2H_4 and the anionic complex. Thus, the large acceleration of nucleophilic attack by the cationic complexes is attributed to the large stabilization from ES and FCTPLX terms and the small destabilization from the EX term. This implies that the palladium-assisted nucleophilic attack might be characterized as a frontierand simultaneously charge-controlled reaction.

Mulliken populations (Table III) and difference density maps (Figure 5) are also analyzed according to the EDA scheme, to investigate how each interaction contributes to electron distribution. As shown in Table III and Figure 5, changes in electron distribution caused by the reaction primarily result from the FCTPLX interaction and to a lesser extent from the EX repulsion. Certainly, the total difference density map can be almost reproduced by a sum of difference density maps of EX and FCTPLX, as shown in Figure 5. These imply that FCTPLX and EX interactions are important from the point of view of the electron distribution. The greater importance of FCTPLX is also indicated by the following results: (1) The FCTPLX term decreases the electron population of NH3 but increases electron populations of both the C_2H_4 moiety and the PdF_nL_{3-n} group. Simultaneously, the electron density decreases near the C^{α} atom and increases near the C^{β} atom through this term. These changes are consistent with the overall changes of the electron distribution. (2) The difference in electron distribution between $[PdF_3(C_2H_4)]^-$ and $[PdF_3(C_2H_4)]^ (PH_3)_2(C_2H_4)$ ⁺ mostly comes from the FCTPLX term (see Table III). (3) Only this term accumulates the electron density between the C^{α} atom and the nucleophile, which corresponds to the formation of a covalent bond between the C^{α} atom and nucleophile (see Figure 5C).

The difference density maps of Figure 5 also shed some light on the nature of the transition state. The EX interaction decreases the electron density in the region between the C^{α} atom and the nucleophile to a greater extent than the FCTPLX interaction increases it (Figure 5B, C). This leads to a net decrease in the electron density between the C^{α} atom and the nucleophile, as shown by the total density map of Figure 5A. In other words, the C^{α} —N bond is not formed effectively near the transition state and the EX repulsion is still strong there. These observations are in accordance with the early transition state of the reaction (vide supra).

Orbital Mixing near the HOMO and LUMO. The above-described changes in electron distribution and the ligand effect on the reactivity are easily explained in terms of the orbital mixing near the HOMO and LUMO,²⁰ which arises from a second-order perturbation among the lone pair of the nucleophile (ϕ_i) and the

^{(20) (}a) Similar orbital mixing has been proposed for the organic reactions^{20b} and the reactions of non transition metals.^{3e} (b) Bach, R. D.; Wolber, G. J. Am. Chem. Soc. **1984**, 106, 1401.



Figure 7. Energy levels of some important orbitals near the HOMO and LUMO of $PdF_nL_{3-n}(C_2H_4)$ and NH_3 ($R_{C^n-N} = 3.0$ Å).

two pairs of bonding and antibonding molecular orbitals $(\phi_{\pi}, \phi_{d\pi}, \phi_{\pi^*}, \phi_{\sigma^*})$ in the palladium–ethylene complex (see Figure 8 for these orbitals^{21a}).

The energy levels of these orbitals are compared at $R_{C^{\circ}-N} = 3.0$ Å (Figure 7). At this distance the nucleophile is considered to be under the influence of the charge in the palladium-ethylene complex but does not effectively form a covalent interaction with the C₂H₄ part. The critical difference in the reaction systems is found with the relative energy levels of the lone pair of NH₃ and the ϕ_{π} , $\phi_{d\pi}$, $\phi_{\pi^{\bullet}}$, $\phi_{\sigma^{\bullet}}$ orbitals of palladium-ethylene complexes. In the cationic complexes, the energy level of the lone-pair orbital lies between those of ϕ_{π} and $\phi_{d\pi}$ orbitals, in the neutral complex between those of ϕ_{π} and $\phi_{d\pi}$ orbitals, and in the anionic complex lower than those of two occupied orbitals, ϕ_{π} and $\phi_{d\pi}$.

This difference in the relative position of the lone pair leads to significantly different orbital mixings, as schematically represented in Figure 8.^{21b} In the cationic complex, the ϕ_1 orbital is mainly composed of the $\phi_{d\pi}$ orbital, into which ϕ_l mixes in a bonding way. The ϕ_{π} , ϕ_{σ^*} , and ϕ_{π^*} orbitals also mix into this orbital, but the extent of their mixings is rather small, because their mixings are caused by the second-order term of perturbation. The ϕ_2 orbital mainly consists of the bonding interaction between ϕ_l and ϕ_{π} orbitals. The mixings of $\phi_{d\pi}$ and ϕ_{σ^*} into this orbital are small, since they arise again from the second-order term through the small overlaps of the $\phi_l - \phi_{\sigma^*}$ and $\phi_l - \phi_{d\pi}$ orbital pairs (note a small p_{π} lobe of the carbon atom in the $\phi_{d\pi}$ and ϕ_{σ^*} orbitals). The ϕ_{π^*} orbital also mixes into the ϕ_2 orbital only a slight amount, since this mixing is caused by the second-order term and ϕ_{π^*} lies much higher in energy than the ϕ_{π} orbital. Thus, ϕ_2 is only slightly perturbed by these mixings, as schematically

⁽a) The coordinate bond of ethylene to palladium is primarily contrib-(21) uted by the σ -donative interaction and secondarily by the π back-donation.²² Thus, the $\phi_{d\pi}$ orbital is considered to be predominantly pal-ladium 4d in character, and ϕ_{π^*} is predominantly π^* orbital in character, as depicted in Figure 8. (b) The orbital mixing of this work is based on the second-order perturbation, as in the orbital mixing of ref 3b. According to our orbital mixing, the $C^{\beta} p_{*}$ orbital is enlarged but the $C^{\alpha} p_{\pi}$ orbital is decreased in the occupied level. This means that in the virtual space the C^{β} p_{τ} orbital is decreased and the C^{α} p_{τ} orbital is enlarged. Such changes found in the virtual space are essentially the same as those obtained in the orbital mixing of ref 3b. However, there are several differences between ref 3b and this work: (1) The orbital mixing is induced by the lone-pair orbital of the nucleophile, NH₃, in our case but by the displacement of olefin from a symmetrical (η^2) coordinating position to an unsymmetrical (η^1 -like) coordinating position in ref 3b. (2) Changes in occupied orbitals are examined in detail here, which clarifies why and how electron distribution and bonding nature change by the nucleophilic attack of NH₃ on the coordinated olefin. In ref 3b, the LUMO of metal-olefin complexes is examined very well, which facilitates the prediction of the reactivity of coordinated olefin from the point of view of frontier orbital theory.



Figure 8. Schematic pictures of orbital mixing caused by the nucleophile.

depicted in Figure 8. The ϕ_3 orbital mainly consists of $\phi_l - \phi_{\pi}$ antibonding and $\phi_l + \phi_{\pi^*}$ bonding, in which the ϕ_{π^*} mixing occurs with the same phase as the $C^{\beta} p_{\pi}$ lobe of ϕ_{π} but with the phase opposite to the $C^{\alpha} p_{\pi}$ lobe of ϕ_{π} . Mixings of the other orbitals, $\phi_{d\pi}$ and ϕ_{σ^*} , are rather small because of their small overlaps with ϕ_l (vide supra). As a result, the ϕ_3 orbital is deformed as follows: the $C^{\beta} p_{\pi}$ lobe becomes large but the $C^{\alpha} p_{\pi}$ lobe becomes small, which strengthens the bonding interaction between Pd and C^{β} atoms and weakens bonding between Pd and C^{α} atoms. These changes in electron distribution and bonding agree well with their overall changes described above, and any of the other orbital mixings in the ϕ_1 and ϕ_2 orbitals do not cause such changes. Of the $\phi_l + \phi_{\pi^*}$ and $\phi_l - \phi_{\pi}$ orbital mixings involved in ϕ_3 , the former mixing is more important to the reaction than the latter, because the $\phi_l + \phi_{\pi^*}$ mixing is bonding between the C^{α} atom and nucleophile. The acceleration by $[PdF(PH_3)_2(C_2H_4)]^+$ being higher than that by the NH₃ analogue can be explained in terms of this orbital mixing. The PH₃ complex exhibits a difference in energy between the ϕ_{π^*} and ϕ_l orbitals smaller than that of the NH₃ analogue by ca. 0.02 eV (see Figure 7), yielding greater mixing of the ϕ_{π^*} orbital into the ϕ_3 orbital. Thus, the PH₃ complex can form a stronger bonding interaction between the nucleophile and the C^{α} atom.

In the neutral complex, the ϕ_3 orbital, shown in Figure 8B, is also important. Unfortunately, however, the difference in energy between ϕ_l and ϕ_{π^*} is 0.60 eV, greater than that of the cationic complex by ca. 0.15 eV, as shown in Figure 7. In the anionic complex, on the other hand, the ϕ_2 orbital becomes important to the reaction as shown in Figure 8C (note that the ϕ_l orbital lies lower in energy than the $\phi_{d\pi}$ and ϕ_{π} orbitals, unlike the case for the neutral and the cationic complexes). Also in ϕ_2 , the $\phi_l + \phi_{\pi^*}$ mixing is included as an important component. Nevertheless, the difference in energy between the ϕ_l and ϕ_{π^*} orbitals is the greatest (0.65 eV; see Figure 7), and therefore, not only the bonding mixing of $\phi_l + \phi_{\pi^*}$ but also the deformation of the ϕ_2 orbital leading to the product is the smallest in the palladium-olefin complexes examined.

The relationship between results of the EDA and orbital mixing is also interesting. If the energy difference between ϕ_{π^*} and ϕ_l is small, the $\phi_{\pi^*} + \phi_l$ mixing becomes large and therby the strong charge transfer from NH_3 to C_2H_4 arises, and vice versa. This charge-transfer interaction is a main part of the FCTPLX term. Because the $\phi_{\pi^*} + \phi_i$ mixing in ϕ_3 reduces the size of the C^{α} p_{π} lobe but enlarges the size of the $C^{\beta} p_{\pi}$ lobe (see Figure 8), this mixing corresponds to the polarization of the C_2H_4 moiety, which is also a part of FCTPLX. The decrease in the $C^{\alpha} p_{\pi}$ lobe weakens the EX repulsion between the nucleophile and the C^{α} atom and simultaneously strengthens the ES interaction between them. In the cationic complexes, especially in $[PdF(PH_3)_2(C_2H_4)]^+$, the difference in energy between ϕ_{π^*} and ϕ_l is the smallest, yielding the greatest mixing of $\phi_{\pi^*} + \phi_l$, the greatest stabilization from FCTPLX and ES terms, and the smallest destabilization from the EX term. In both neutral and anionic complexes, the difference in energy is rather large, which leads to smaller stabilization from the FCTPLX and ES terms and larger destabilization from the EX term.

Ligand Effect on the Reactivity. These results are suggestive for the ligand that facilitates metal-assisted nucleophilic attack. From the point of view of the EX and FCTPLX interactions, the metal and ligand that stabilize ϕ_{π^*} are desirable, since the smaller difference in energy between ϕ_l and ϕ_{π^*} orbitals leads to greater orbital mixing of ϕ_{π^*} . The ϕ_{π^*} orbital involves an antibonding interaction between the palladium $d\pi$ and $C_2H_4 \pi^*$ orbitals, and therefore, a weak back-donative interaction between the palladium $d\pi$ and $C_2H_4 \pi^*$ orbitals results in ϕ_{π}^* lying lower in energy. Palladium(II) complexes have been experimentally shown to exhibit a slight ability to form a π -back-donative interaction.²² The present MO calculations also indicate that the back-donative interaction is weaker than the donative interaction except for [PdF₃(C₂H₄)]⁻ (see Table I).

Not only the metal but also the ligand influences the energy of the ϕ_{π^*} orbital. As clearly shown in Figure 7, an anionic ligand pushes up the ϕ_{π^*} orbital via electrostatic repulsion. Thus, an anionic ligand disfavors the metal-assisted nucleophilic attack.

From the point of view of charge control the ES interaction is important. As discussed in Table I, the FCTPLX interaction from C_2H_4 to Pd is the weakest in $[PdF_3(C_2H_4)]^-$, probably owing to the high-lying acceptor orbital of palladium pushed up by electrostatic repulsion from the anionic F⁻ ligand. In the case of a neutral soft ligand, such as PH_3 , the electron donation from C_2H_4 to Pd is the greatest, making the ethylene ligand the most positively charged and thereby yielding the greatest stabilization of the ES interaction.

Basis Set Superposition Error (BSSE) and Electron Correlation Effects. The corrections for BSSE²³ and electron correlation effects are briefly examined for a simple model system, [PdF- (C_2H_4)] \leftarrow NH₃. Electron correlation, estimated with the MP2 method,²⁴ stabilizes the transition state by about 8 kcal/mol, compared to the structure at $R_{C^{\alpha}-N} = 3.0$ Å. On the other hand, the BSSE value at the transition state was estimated to be larger than that at $R_{C^{\alpha}-N} = 3.0$ Å by about 5 kcal/mol.²⁵ Because of the large size of the reaction system, a polarization function on the N atom of the nucleophile was not included in the basis set. The effect of the polarization function^{9b} was also investigated in the $C_2H_4 \leftarrow NH_3$ system and estimated to destabilize the transition state by about 2 kcal/mol compared to the structure at $R_{C^{\alpha}-N}$ = 3.0 Å. Of course, the effect of the polarization function is somewhat different for $[PdF(C_2H_4)]^{-}$ NH₃. Nevertheless, the result is considered to be correct in a qualitative sense. The sum of the correction for the activation barrier is about -1 kcal/mol; the MP2 correction (-8 kcal/mol) plus the BSSE correction (+5 kcal/mol) plus the correction by the polarization function (+2)kcal/mol). Although the consideration of these terms is only qualitative, they do not appear to make a sizable contribution. A more detailed examination of these corrections will be carried out in the near future.

Conclusion

Palladium-assisted nucleophilic attack on a coordinated olefin has been investigated with an ab initio MO method and energy decomposition analysis. The cationic palladium(II)-ethylene complex is proposed as an active species, which agrees with experimental evidence. The activation barrier is calculated to be about 6-8 kcal/mol at the Hartree-Fock level. This value is not expected to change very much when corrected for BSSE and electron correlation effects. The rather low activation barrier seems in accordance with the extreme facility of this reaction. The semiquantitative features of the reaction including changes in geometry and electron distribution are clearly obtained and explained on the basis of orbital mixing. The detailed analysis of those changes suggests that this reaction has a rather early transition state. From the energy decomposition analysis of the interaction between the nucleophile and the palladium-ethylene complex, the origin of the palladium acceleration may be attributed to the large stabilization of ES and FCTPLX and the small destabilization of EX. Thus, the palladium-assisted nucleophilic attack is considered to include characteristics of both frontier control and charge control. From both points of view, neutral and soft ligands favor nucleophilic attack.

Acknowledgment. All calculations were carried out by using the Hitac M-200H, M680, and S810 computers of the Computer Center of the Institute for Molecular Science (IMS), through a Joint Studies Program of the IMS. We are grateful to Prof. K. Morokuma and Dr. N. Koga for their interest and generous support and to the Ministry of Education for financial support through Grant-in-Aids.

Registry No. 1, 52314-09-7; 2, 108969-67-1; 3, 108969-68-2; 4, 108969-69-3.

 ⁽²²⁾ Calderazzo, F.; Dell'Amico, D. B. Inorg. Chem. 1981, 20, 1310. Uson, R.; Forniés, J.; Tomas, M.; Menjón, B. Organometallics 1985, 4, 1912.

 ⁽²³⁾ The BSSE value was estimated by the counterpoise method: Boys, S. F.; Bernardi, F. Mol. Phys. 1970, 19, 553. Ostlund, N. S.; Merrifield, D. L. Chem. Phys. Lett. 1976, 39, 612.

 ⁽²⁴⁾ The frozen-core approximation was applied, in which the 1s-3s, 2p-3p, and 3d orbitals of palladium and the 1s orbital of the first-row atoms are included in core orbitals.

⁽²⁵⁾ This type of correction tends to overestimate the BSSE value. However, such an overestimation is not so large here because we discuss only the difference in BSSE between two structures at $R_{C^{\alpha}-N} = 3.0$ and 2.0 Å.